

Introduction

The field of computational particle modeling has proven imperative in initializing and controlling the motion of particles in plasma machines like tokamaks and stellarators. Physicists have obtained a firm understanding of smaller particle systems, like the "Two-Body Problem", as well as massive ones, from the empirical data from galaxies. The gravitating systems of the tens, hundreds, and thousands range, however, still introduce an element of uncertainty. In order to better understand the nature of these particle interactions, we decided to design a symplectic integrator under the leapfrog scheme to model the location and energies of self-gravitating systems.



The middle-range (10s, 100s, 1000s)

To improve the accuracy of our integrator, we also implemented an adaptive time-stepping algorithm in our C code that reduces the time step whenever at least one particle is moving too fast and increases the time step whenever every particle is moving slowly. Finally, we worked to animate the plots, finally being able to demonstrate the motion of five of the particles in the eight-body test traversing about 330,000 data points in less than 10 seconds, giving users a reliable framework to observe the results of their simulations.

Simple Harmonic Oscillator

To test the feasibility of using the leapfrog scheme, we started by modeling the motion and energy of a simple harmonic oscillator (SHM), modeled under a second-order leapfrog scheme. The position and energy of the plots were computed and plotted in Python. The location plot ended up being very accurate, but the energy plot was sinusoidal, instead of constant, marking a key characteristic in most adaptations of the leapfrog integrator^[2].



References

[1]: ESA/Hubble & NASA, D. Rosario et al.

[2]: Time-Reversibility. (n.d.). Retrieved August 18, 2020, from http://www.physics.drexel.edu/~valliere/PHYS305/Diff_Eq_Integrators/time_reversal/

An Adaptive Symplectic Integrator for Modeling the Mechanics of Self-Gravitating Systems

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Two/Three-Body Problem Tests



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